

Using Multidimensional Skylines for Regret Minimization

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Context

- Investigate Top-K frequent and Top-K priority skylines as candidate sets for regret minimization queries¹
- Experiment the speedup provided by NSC(Negative Skycube)² to regret minimization queries

[1] D. Nanongkai, A. D. Sarma, A. Lall, R. J. Lipton, and J. Xu. Regret-minimizing representative databases. *Proceedings of the VLDB Endowment*, 3(1-2):1114–1124, 2010.

[2] Alami, K., Hanusse, N., Kamnang-Wanko, P., & Maabout, S. (2020). The negative skycube. *Information Systems*, 88, 101443.

Preference queries

Given a set of tuples T , it returns a subset of tuples that suits the user preference

- Top-K query: based on scoring function
- Skyline query: based on dominance

Hotel	Price	Distance
h_1	75	100
h_2	45	150
h_3	50	300
h_4	65	450
h_5	25	500
h_6	50	400
h_7	100	150
h_8	30	300

E.g

- Skyline query result:
 h_1, h_2, h_5 and h_8

- Top-2 query result:
Scoring function $f(t) = P + D$
 h_1, h_2

Regret minimization query

Limitations

- Top-K query: requires to define a scoring function
- Skyline query: the size of the output is not controlled

Regret minimization query¹: bounds the output without requiring a scoring function

We consider L the family of linear scoring function

Let $f \in L$, $f_1(T)$ the highest score

- Given $S \subset T$ the maximum regret ratio, $\text{mrr}(S, L) = \max_{f \in L} \frac{f_1(T) - f_1(S)}{f_1(T)}$

Problem RMS: Given a dataset T , the family of linear function L , an integer r , compute a set $S \subset T$ of size r that minimizes the maximum regret ratio $\text{mrr}(S, L)$

The regret represents how much users are satisfied with S .

Regret minimization query

RMS is NP Hard¹

*sphere*² is the state of the art heuristic algorithm with guarantees

Skyline points as candidates

Let Sky be the skyline set of T . Let S^* be the optimal solution of an RMS instance such that $r \leq |Sky|$, then $S^* \subseteq Sky$

[1] S.Chester,A.Thomo,S.Venkatesh,andS.Whitesides.Computingk-regret minimizing sets. *Proc. VLDB Endow.*, 7(5):389–400, 2014

[2] M. Xie et al.. Efficient k-regret query algorithm with restriction-free bound for any dimensionality. *Proceedings of SIGMOD Conference 2018*

Multidimensional Skylines

Skyline set may be of the size of the whole dataset

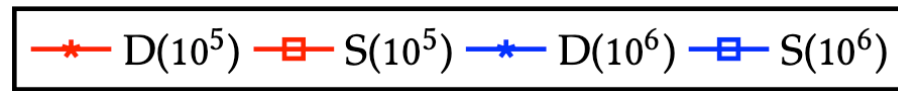
We investigate Top-K Frequent skylines and Top-K priority skyline as candidate sets¹

Top-K Frequent (Top-KF)	Top-K Priority (Top-KP)
Frequency: the number of subspaces ² where a tuple is in the skyline	Priority: the cardinality of the smallest subspace where a tuple is in the skyline

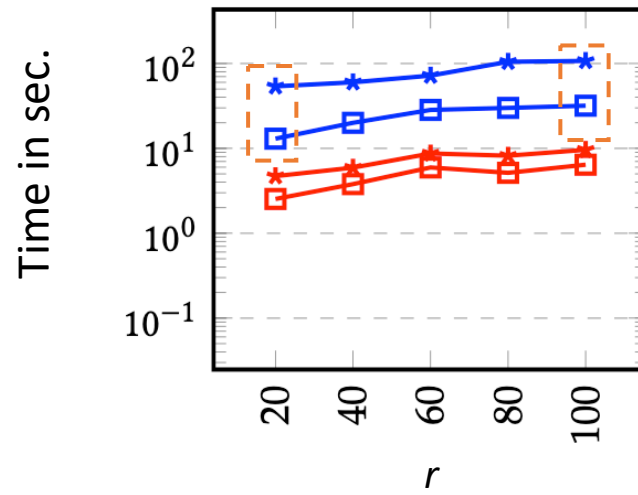
[1] We compute Top-KF and Top-KP with index structure NSC

[2] Subspace: subset of dimensions

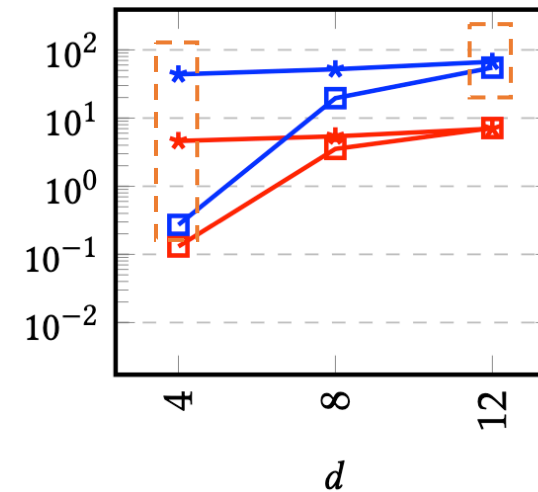
Speedup with skyline candidate set



$d = 8$

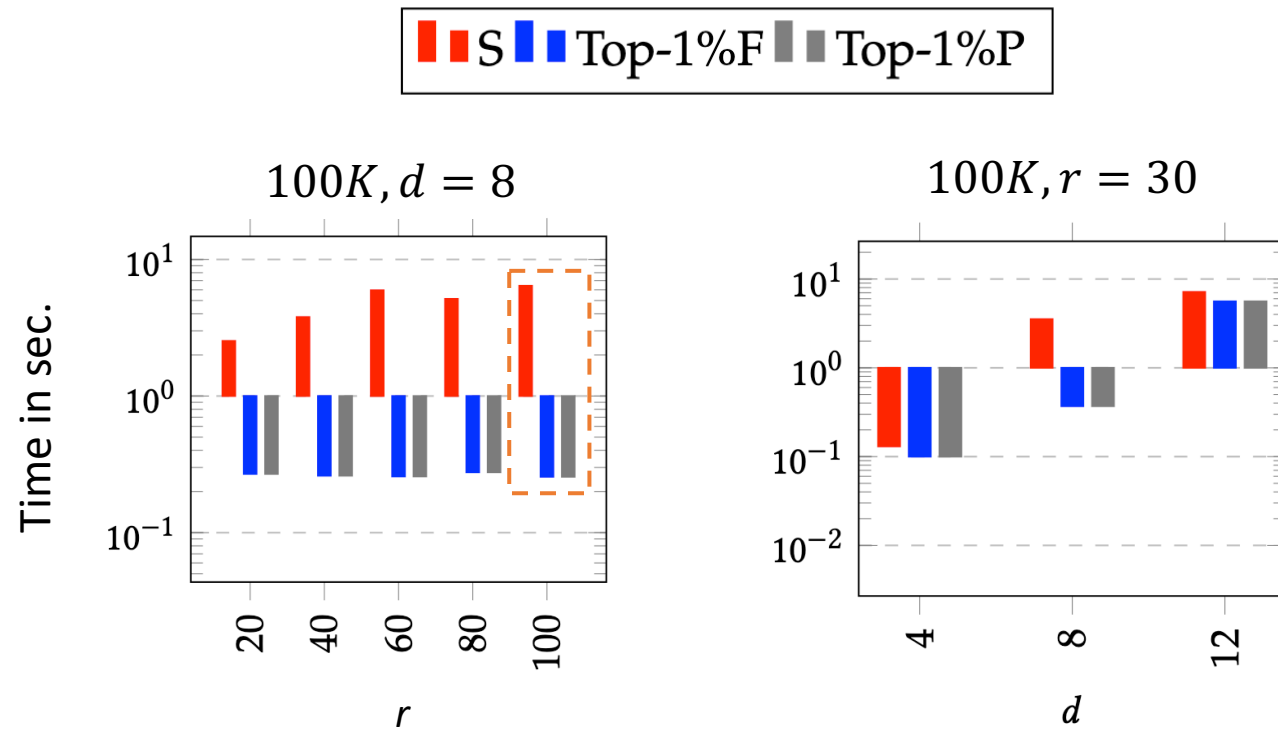


$r = 30$



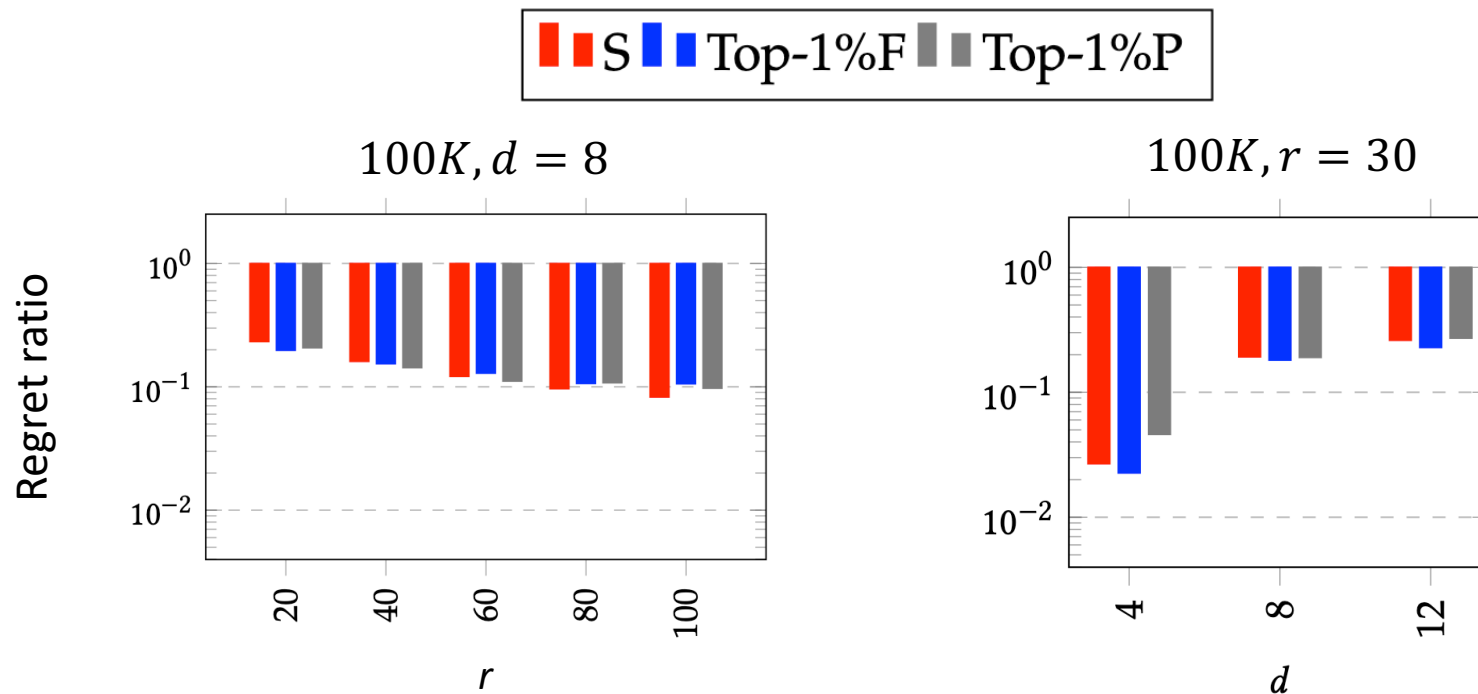
r : size of the output by sphere
 d : number of dimensions
 D : dataset
 S : Skyline set

Speedup with Top-KF and Top-KP



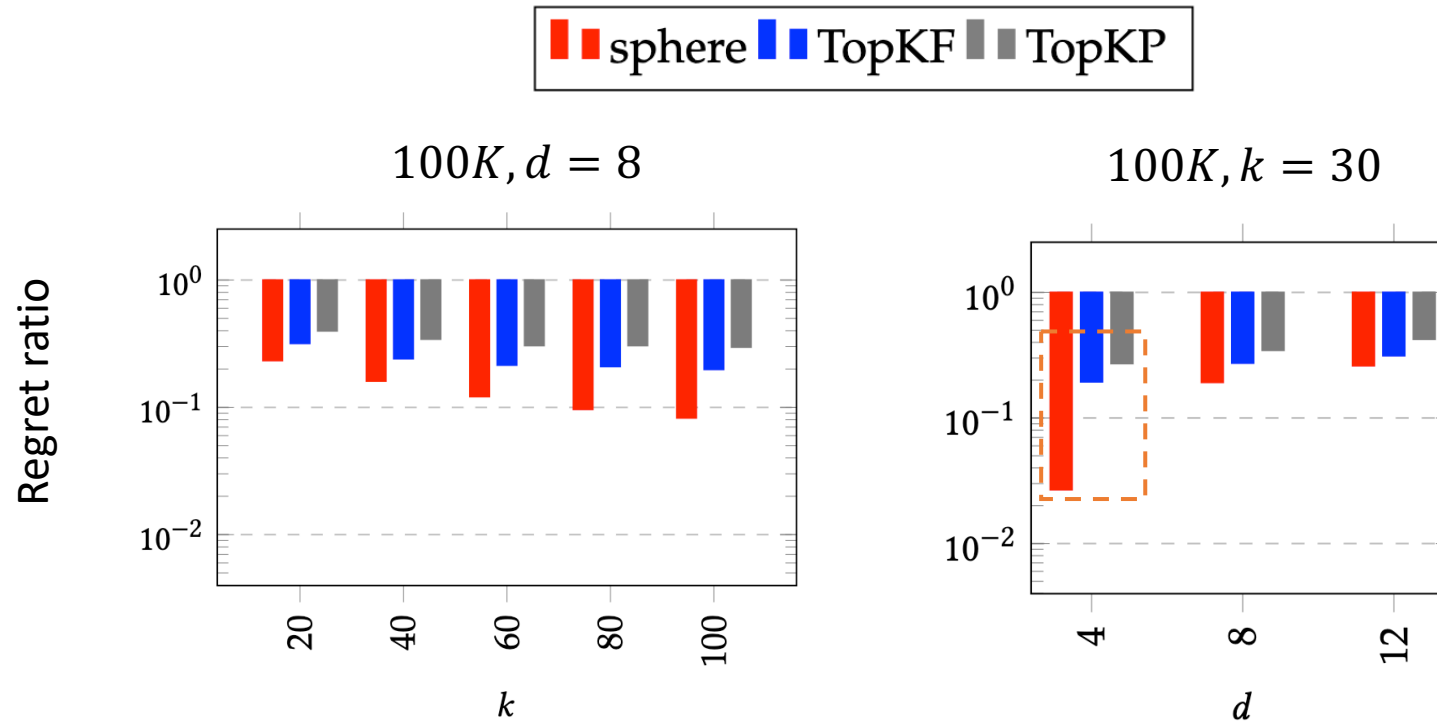
r: size of the output by sphere
d: number of dimensions

Regret ratio with Top-KF and Top-KP



r : size of the output by sphere
 d : number of dimensions

Regret ratio of *sphere* vs Top-KF vs Top-KP



k : size of the output by *sphere*, TopKF, and TopKP
 d : number of dimensions

Conclusion and Perspectives

Conclusion:

- Top-KF computes a good candidate set for *sphere*
- NSC speedup *sphere* by optimizing the computation of candidate sets

Perspective:

- A theoretical guarantee on the regret ratio by using the candidate sets Top-KF and Top-KP

Questions